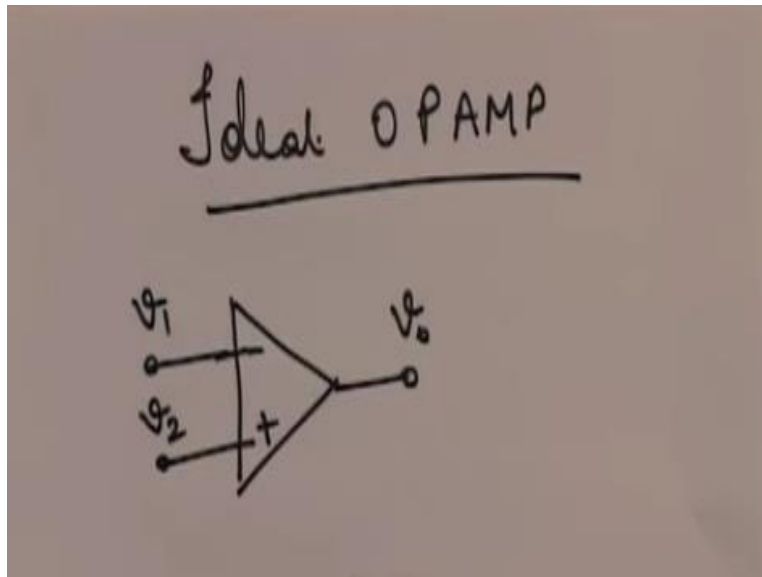


**Analog Circuits**  
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**Week -01**  
**Module -04**  
**Applications of Op-Amps**

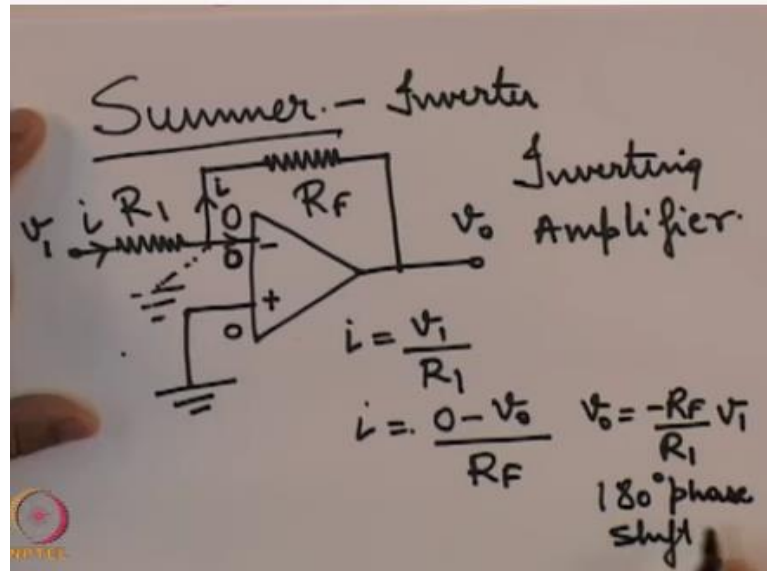
Hello, welcome to another module of this course analog circuits. In the last module, we had introduced you to the concept of an opamp, what is an opamp? What are its properties especially that of an ideal opamp. In this module we shall be seeing some applications of the ideal opamp.

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So once again, if we draw the circuit of an ideal opamp so 3 port device  $v_o$ ,  $v_1$ ,  $v_2$  so this is the inverting this is the non inverting port.

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Now let us see one first application which is the summer, this is the basic circuit of a summer or more precisely what we call a summer inverter also known as an inverting amplifier, why it is called an inverting amplifier? It will become clear if we see the equations now, see that the non inverting terminal is grounded but the inverting terminal is not grounded, now since this is an ideal opamp there is a virtual short present between the inverting and non inverting terminal.

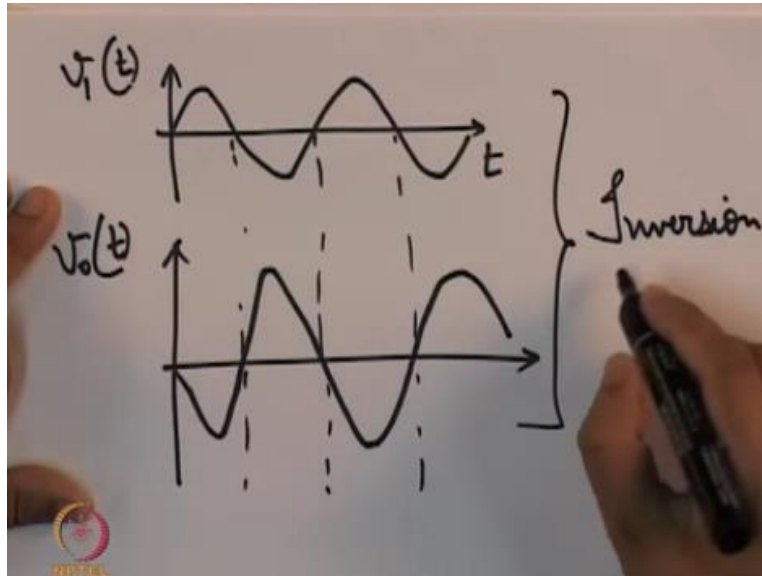
Therefore the voltage here is 0, the voltage here is also 0, if this is 0 voltage then that means there is a material called a virtual short and virtual short means that whatever be the input voltage this point will keep on acting like a short, it is not really connected to the ground but it is for all practical purposes it acts like a short, because this voltage will always be the same as this voltage which is 0.

So now if we write the current  $i$  that will be given by  $v_1$  over  $R_1$  and also we know that the input impedance of an opamp is infinity so the current flowing inside opamp is 0 therefore all the current coming flowing through  $R_1$  will be diverted to this path and hence the current along this path is also  $i$ .

So, we can say that now what is the current flowing through this resistance  $R_f$ , it is the same as this current but what is the value in terms of  $R_f$  can we write that  $i$  is equal to this voltage - this voltage upon the resistance so then  $i$  equal to  $0 - v_o$  upon  $R_f$  now equating the 2 we get  $v_o$  is equal

to  $-R_f$  upon  $R_1 v_1$  that is it now it is called an inverting amplifier because the output is the negative of the input negative of the input also means invert like 180 degree phase shift.

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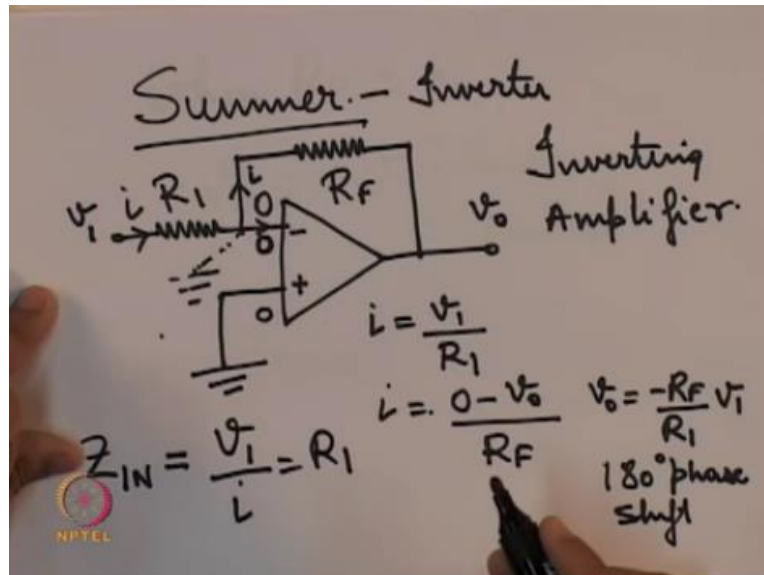
So if suppose our  $v_1$  is a sinusoidal signal then it will look something like this, we plot the input that is  $v_1$  as a function of time like this then the output which is usually amplified will be the inverse of this, so where it is positive it will become negative and where it is negative it will become positive and so on so because of this inversion or this 180 degree phase shift we call amplifier as inverting amplifier.

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$$\text{When } R_f = R_1$$
$$v_0 = -v_1 \left. \vphantom{v_0} \right\} \begin{array}{l} \text{Unity gain} \\ \text{inverter} \end{array}$$

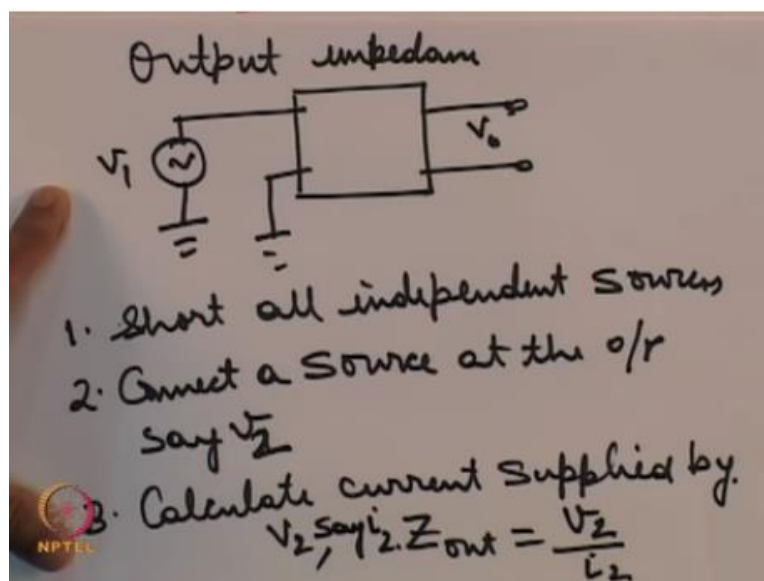
A special case arises when  $R_f$  is equal to  $R_1$  then  $v_o$  will simply be the negative of  $v_1$  and such a configuration is called unity gain inverter so all this inverter does is change the sign or introduce a phase shift.

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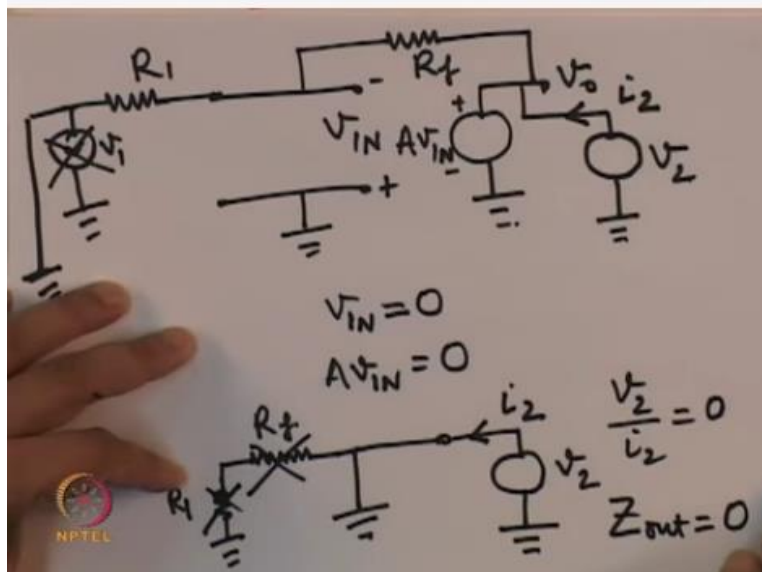
Now if I ask you to find out the input impedance of this configuration, so let us go back to our circuit, so to find out input impedance what you do is you calculate the input voltage over the input current so  $Z_{in}$  is equal to  $v_1$  over  $i$  and that is simply equal to  $R_1$ , we can also try to calculate the output impedance output impedance of any amplifier.

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Suppose this is a general rule to calculate the output impedance, what we do is suppose you have a source or many sources feeding this amplifier and you are taking output between certain points then the way to find out the output impedance is to short all independent sources number 1, number 2 connect a source at the output say  $v_1$  or let us say  $v_2$  calculate current supplied by  $v_2$  then your output impedance is equal to  $v_2$  by  $i_2$  say that current  $i$  call it as  $i_2$ .

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Ok, so in the case of an opamp what is let us go back to the equivalent circuit that we discussed in the previous class, so the equivalent circuit of an opamp is given like this okay now here or it is  $v$  now here we have connected a resistance  $R_1$ , ok this terminal this is the non-inverting terminal which is grounded and between these 2 terminals.

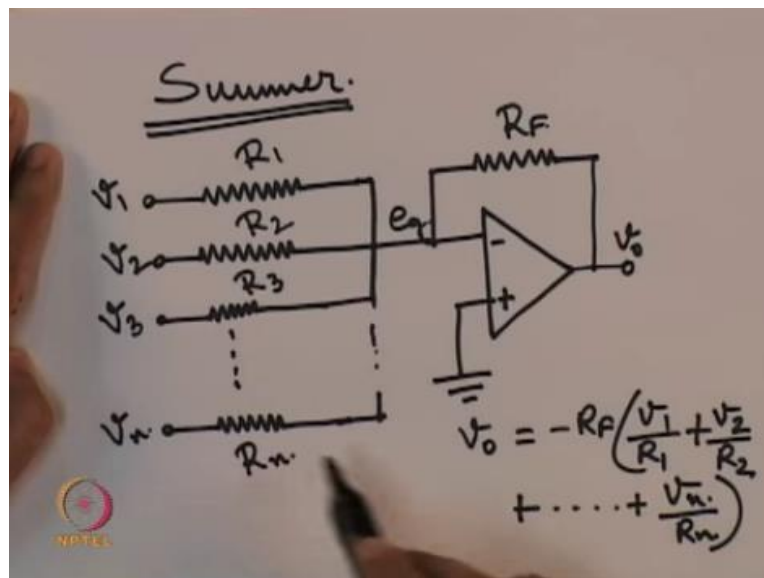
We have our  $R_f$  so this the  $v_o$  terminal okay now when I say so the first step is to short this if I short this then this gets cancelled and we have this terminal directly connected to ground, so if this terminal is connected to ground and this terminal is connected to ground and here at the output we connect the source let us say that is  $v_2$  and suppose the current supplied by  $v_2$  is  $i_2$  then if we can compute what is the value of  $i_2$  we shall be able to calculate the value of the output impedance.

Now first thing note that because this source voltage is now 0, so we can say that  $V_{in}$  that is the voltage actually appearing at the input and the non inverting terminal is 0  $V_{in}$  is 0 then this  $A V_{in}$

is also equal to 0, so in that case the equivalent circuit becomes something like this now this  $R_f$  and  $R_1$  which are in series is shunt to this short this terminal is shorted directly here so then the effect of these resistance go away and therefore  $v_2$  upon  $i_2$  becomes equal to 0, since this is a short so the output impedance is therefore equal to zero for an inverting amplifier.

Now the next application of this is in the same way now this particular configuration that we discussed this was with a single source present but you may have a number of inverting sources or sources present which have to be uh amplified so the circuit for that is or what we called as summer.

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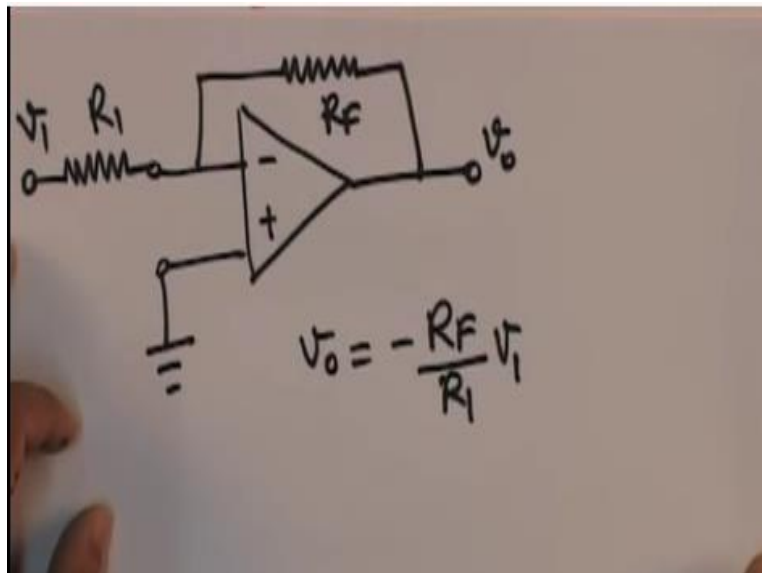
In the previous case we just talked about an inverting amplifier, but what if we have a number of such signals then we get a circuit what is called the summer which was the original topic that we are discussing now. So in the circuit for that is this is the circle now here what we have is this all voltage sources  $v_1$  till  $v_n$  connected in shunt and then the shunt at the point where they are all joint is fed to the inverting input of an opamp.

Now the first thing is that the  $v_o$  is very simply can be written as  $-R_f$  upon  $v_1$  by  $R_1$ +  $v_2$  upon  $R_2$ + till  $v_n$  upon  $R_n$ , how did we obtain this result so here we apply the principles of superposition, superposition means since this is a linear system the effect of all the sources will be the sum of the effects of individual sources acting at a time.

So assume at the beginning we have only  $v_1$  connected and all the sources are not connected other sources are not connected then what it means is that these  $R_2, R_3$  till  $R_n$  they are simply floating and therefore they do not contribute anything to the output, in that case the output will be if only  $v_1$  is connected with simply be  $-R_f$  upon  $R_1$  times  $v_1$  similar will be the result for the other sources.

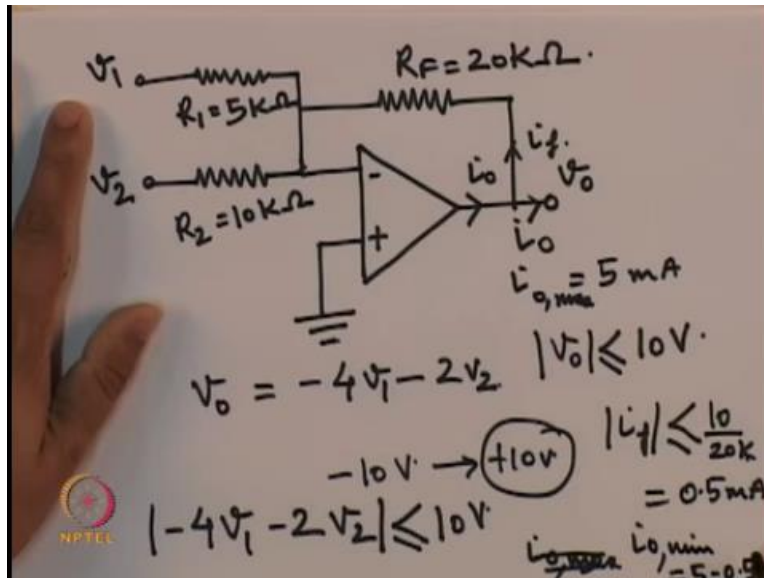
For example, when only  $v_2$  is connected the output will be  $-R_f$  upon  $R_2$   $v_2$  and so on and finally so the overall impact on  $v_o$  will be the sum of the impacts produced by these individual sources and that is how we get this sum.

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One thing that we are not so far considered is the current that is being sourced at the output of the open what I mean is suppose we have an opamp in an inverting configuration the relationship between  $v_o$  and  $v_1$  is like this so from this it appears as if the only the ration of  $R_f$  and  $R_1$  that is what matters individual values of  $R_f$  and  $R_1$  do not matter, but is it so?

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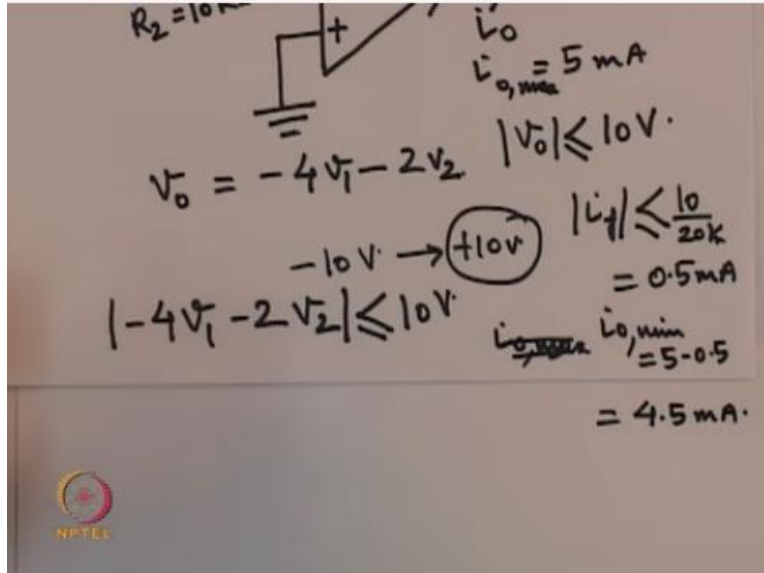


Let us see with an example suppose we have summer in this configuration, now as we can see  $V_o$  will be given by  $-4v_1-2v_2$  now suppose the maximum current that can be sourced say the maximum current that can be provided at the output of this opamp is say 5 m 5 milli ampere so  $i_{o,max}$  is say equal to 5mA milli ampere and say the maximum output voltage that can be provided at the output is equal to 10 volts now this maximum output voltage this concept comes from the saturation voltage of the device used.

For example in any this is after all a practical circuit so this might have been built with some BJT's or MOSFET's, by BJT I mean bipolar junction transistor and MOSFET I mean a metal oxide semiconductor field effect transistor whichever device we use they have a certain maximum output voltage and a minimum of it usually the maximum output voltage that can be supplied by a device is the upper rail or the upper value of the power supply.

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For example, if your power supply is between -10 volts to +10 volts then this +10 voltage will be the upper rail of the power supply and this is the maximum output voltage that can be provided and similarly this -10 volt is the lower rail of the output voltage and this is the minimum voltage that can be provided in this case this is the way it is, so  $v_o$  magnitude is lesser than 10 volts so we have the rail to rail output voltage will be between -10 volts to +10 volts.

Now if this is the case then what it means is since  $v_o$  is given by this relationship it means that  $-4v_1 - 2v_2$  modulus will be lesser or equal to 10 volts now in the worst case we will have an  $i_f$  or the current flowing from this to this resistance that is if the output voltage is at its maximum then  $i_f$  the current that is flowing through  $R_f$  the maximum value that will be reached is 10 divided by 20K which is equal to 0.5 milliampere, so  $i_f$  max the maximum value of this is 0.5 mA and  $i_f$  will be magnitude of  $i_f$  will be lesser than this value

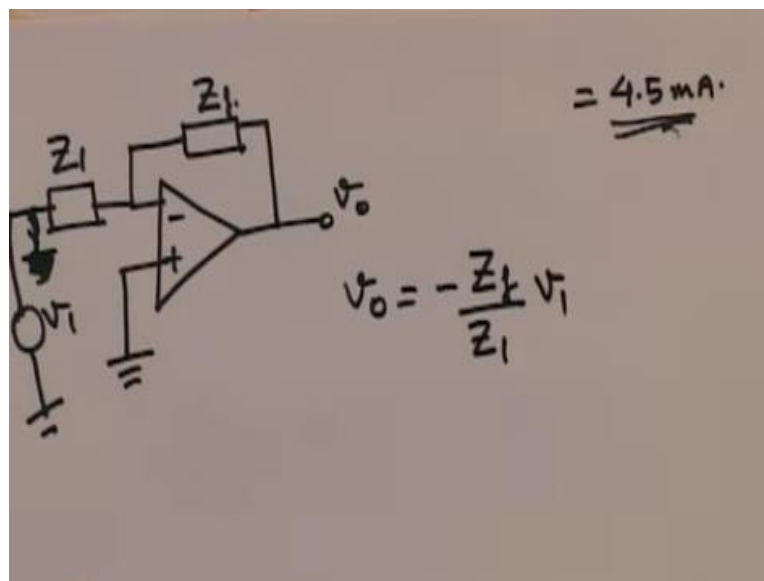
So if that is the case then suppose we are assuming the maximum current is being fed to do this  $R_f$  which is 0.5 mA and the maximum current that can be supplied by this opamp is 5 milliampere, then what is the maximum current that can be supplied to the next stage that is  $I_o$  then  $i_{o,max}$  or  $I_o$  should say it is the minimum sorry because  $i_f$  will be lesser than 0.5 will be equal to 5 - 0.5 which is equal to 4.5, so this is the maximum or the minimum current that will always be present.

Of course, if no current is flowing through this  $R_f$  then in that case the current the maximum the current that can be supplied to the output will be the full value of  $I_o$  which is 5 milli ampere, so this is the minimum current that can always be ensure at the output this example shows that if the current sourcing ability of the opamp is also an important parameter.

So our  $R_f$  values for example, say in this case if our requirement was indeed so suppose our requirement at the output of the opamp is there such that we have to keep on supplying 4.5 m milli amperes of current always, then in that case this  $R_f$  value cannot be lower than 20 kilo ohms if it is lower than 20 kilo ohms then the current supplied through  $R_f$  will increase and it will make the current that can be sourced to the next stage lesser than 4.5 mA.

So, this is where the value of  $R_f$  comes into play and there will be other such restrictions on the performance of opamp due to which  $R_f$  and  $R_1$  will have to be adjusted properly, so it is not just the ratio of  $R_f$  to our one that matters it is also the individual values that matters.

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Taking forward this concept, if we have a general impedance  $Z_1$  and a general impedance  $Z_f$  connected like this will be this will not be like this will be connected to  $v_1$  so then for any in the previous case we had derived the relationship between  $V_o$  and  $v_1$  for resistance is only but in place of resistances if we have general impedances  $Z_1$  and  $Z_f$  then  $v_o$  will be given by  $Z_f$  upon

$Z1 v1$  so using this formula we can derive some special circuits like integrators which we shall be discussing in the next module, thank you.